I Semester

CALCULUS AND DIFFERENTIAL EQUATIONS			
Course Code	21MAT11	CIE Marks	50
Teaching Hours/Week (L:T:P:S)	2:2:0:1	SEE Marks	50
Total Hours of Pedagogy	40	Total Marks	100
Credits	03	Exam Hours	03

Course objectives: The goal of the course Calculus and Differential Equations - 21MAT11 is

- To facilitate the students with a concrete foundation of differential calculus
- To solve the first and higher-order ordinary differential equations enabling them to acquire the knowledge of these mathematical tools.
- To develop the knowledge of matrices and linear algebra in a comprehensive manner.

Teaching-Learning Process (General Instructions):

These are sample Strategies, which teachers can use to accelerate the attainment of the various course outcomes.

- 1. In addition to the traditional lecture method, different types of innovative teaching methods may be adopted so that the delivered lessons shall develop student's theoretical and applied mathematical skills.
- 2. State the need for Mathematics with Engineering Studies and Provide real-life examples.
- 3. Support and guide the students for self-study.
- 4. You will also be responsible for assigning homework, grading assignments and quizzes, and documenting students' progress.
- 5. Encourage the students for group learning to improve their creative and analytical skills.
- 6. Show short related video lectures in the following ways:
 - As an introduction to new topics (pre-lecture activity).
 - As a revision of topics (post-lecture activity).
 - As additional examples (post-lecture activity).
 - As an additional material of challenging topics (pre-and post-lecture activity).
 - As a model solution of some exercises (post-lecture activity).

Module-1: Differential Calculus - 1

Polar curves, angle between the radius vector and the tangent, angle between two curves. Pedal equations. Curvature and Radius of curvature - Cartesian, Parametric, Polar and Pedal forms. Problems.

Self-study: Center and circle of curvature, evolutes and involutes.

(**RBT Levels: L1, L2 and L3**)

0 0	Chalk and talk method / Power Point Presentation
Module-2: Differential Calculus - 2	

Taylor's and Maclaurin's series expansion for one variable (Statement only) – problems. Indeterminate forms-L'Hospital's rule. Partial differentiation, total derivative-differentiation of composite functions. Jacobian and problems. Maxima and minima for a function of two variables. Problems.

Self-study: Euler's Theorem and problems. Method of Lagrange undetermined multipliers with single constraint.

(RBT Levels: L1, L2 and L3)

Teaching-Learning Process	Chalk and talk method / Power Point Presentation

Module-3: Ordinary Differential Equations (ODE's) of first order

Linear and Bernoulli's differential equations. Exact and reducible to exact differential equations. Applications of ODE's-Orthogonal trajectories, Newton's law of cooling.

Nonlinear differential equations: Introduction to general and singular solutions; Solvable for p only; Clairaut's equations, reducible to Clairaut's equations. Problems.

Self-Study: Applications of ODE's: L-R circuits. Solvable for x and y.

(RBT Levels: L1, L2 and L3)

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Teaching-Learning Process	Chalk and talk method / PowerPoint Presentation	
Module-4: Ordinary Differential Equations of higher order		
Higher-order linear ODE's with constant coefficients - Inverse differential operator, method of		
variation of parameters, Cauchy's and Legendre homogeneous differential equations. Problems.		
Self-Study: Applications to oscillations of a spring and L-C-R circuits.		
(RBT Levels: L1, L2 and L3)		
Teaching Learning Process	Chalk and talk method / Power Point Presentation	
Module-5: Linear Algebra		
Elementary row transformation of a matrix, Rank of a matrix. Consistency and Solution of system of		
linear equations; Gauss-elimination method, Gauss-Jordan method and Approximate solution by		
Gauss-Seidel method. Eigenvalues and Eigenvectors-Rayleigh's power method to find the dominant		
Eigenvalue and Eigenvector.		
Self-Study: Solution of system of equations by Gauss-Jacobi iterative method. Inverse of a square		
matrix by Cayley- Hamilton theorem.		
(RBT Levels: L1, L2 and L3).		
Teaching Learning Process	Chalk and talk method / Power Point Presentation	

Course outcomes (Course Skills Set)

After successfully completing the course, the student will be able to understand the topics.

- Apply the knowledge of calculus to solve problems related to polar curves and its applications in determining the bentness of a curve.
- Learn the notion of partial differentiation to calculate rate of change of multivariate functions and solve problems related to composite functions and Jacobian.
- Solve first-order linear/nonlinear ordinary differential equations analytically using standard methods.
- Demonstrate various models through higher order differential equations and solve such linear ordinary differential equations.
- Test the consistency of a system of linear equations and to solve them by direct and iterative methods.

Assessment Details (both CIE and SEE)

The weightage of Continuous Internal Evaluation (CIE) is 50% and for Semester End Exam (SEE) is 50%. The minimum passing mark for the CIE is 40% of the maximum marks (20 marks). A student shall be deemed to have satisfied the academic requirements and earned the credits allotted to each subject/ course if the student secures not less than 35% (18 Marks out of 50) in the semester-end examination(SEE), and a minimum of 40% (40 marks out of 100) in the sum total of the CIE (Continuous Internal Evaluation) and SEE (Semester End Examination) taken together

Continuous Internal Evaluation:

Three Unit Tests each of **20 Marks (duration 01 hour**)

- 1. First test at the end of 5^{th} week of the semester
- 2. Second test at the end of the 10^{th} week of the semester
- 3. Third test at the end of the 15^{th} week of the semester

Two assignments each of 10 Marks

- 4. First assignment at the end of 4th week of the semester
- 5. Second assignment at the end of 9th week of the semester

Group discussion/Seminar/quiz any one of three suitably planned to attain the COs and POs for **20 Marks (duration 01 hours)**

for 20 Marks (duration 01 hours)

6. At the end of the 13^{th} week of the semester

The sum of three tests, two assignments, and quiz/seminar/group discussion will be out of 100 marks and will be **scaled down to 50 marks**

(to have less stressed CIE, the portion of the syllabus should not be common /repeated for any of the methods of the CIE. Each method of CIE should have a different syllabus portion of the course).

CIE methods /question paper is designed to attain the different levels of Bloom's taxonomy as per the outcome defined for the course.

Semester End Examination:

Theory SEE will be conducted by University as per the scheduled timetable, with common question papers for the subject (**duration 03 hours**)

- 1. The question paper will have ten questions. Each question is set for 20 marks.
- 2. There will be 2 questions from each module. Each of the two questions under a module (with a maximum of 3 sub-questions), **should have a mix of topics** under that module.

The students have to answer 5 full questions, selecting one full question from each module

Suggested Learning Resources:

Text Books

- 1. B. S. Grewal: "Higher Engineering Mathematics", Khanna publishers, 44th Ed.2018
- 2. E. Kreyszig: "Advanced Engineering Mathematics", John Wiley & Sons, 10th Ed. (Reprint), 2016.

Reference Books

- 1. V. Ramana: "Higher Engineering Mathematics" McGraw-Hill Education, 11th Ed.
- 2. Srimanta Pal & Subodh C. Bhunia: "Engineering Mathematics" Oxford University Press, 3rd Reprint, 2016.

- 3. **N.P Bali and Manish Goyal**: "A textbook of Engineering Mathematics" Laxmi Publications, Latest edition.
- 4. **C. Ray Wylie, Louis C. Barrett:** "Advanced Engineering Mathematics" McGraw Hill Book Co.Newyork, Latest ed.
- 5. **Gupta C.B, Sing S.R and Mukesh Kumar:** "Engineering Mathematic for Semester I and II", Mc-Graw Hill Education(India) Pvt. Ltd 2015.
- 6. **H.K.Dass and Er. Rajnish Verma:** "Higher Engineering Mathematics" S.Chand Publication (2014).
- 7. James Stewart: "Calculus" Cengage publications, 7th edition, 4th Reprint 2019.

Web links and Video Lectures (e-Resources):

- <u>http://.ac.in/courses.php?disciplineID=111</u>
- <u>http://www.class-central.com/subject/math(MOOCs)</u>
- <u>http://academicearth.org/</u>
- VTU e-Shikshana Program
- VTU EDUSAT Program

Activity-Based Learning (Suggested Activities in Class)/ Practical Based learning

- Quizzes
- Assignments
- Seminars